

# Investigating the use of light diffraction for the closed-loop control of heliostats

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# Overview

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- Introduction
- Background
- Diffraction
- Method
- Conclusion

# Introduction



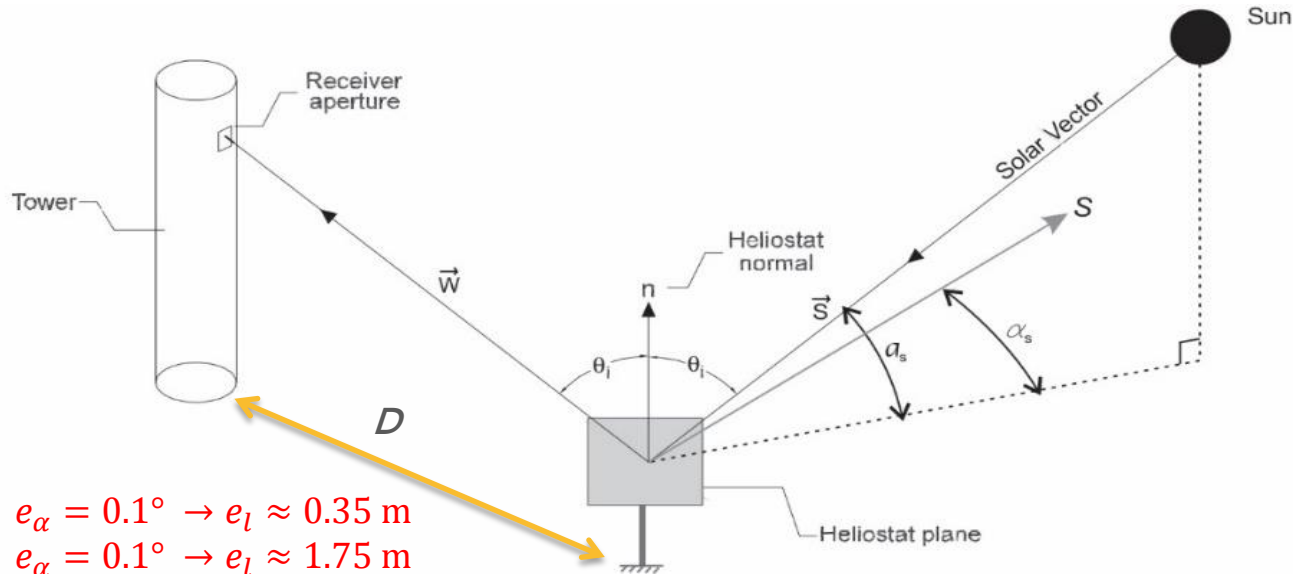
- Heliostats in Central Receiver Systems



# Introduction



- Aiming Problem



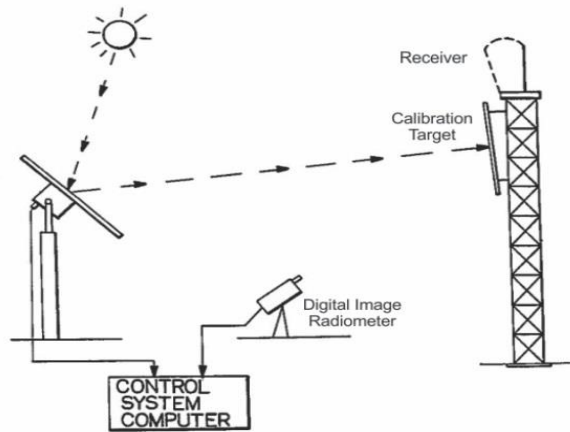
$D = 0.2 \text{ km}: e_\alpha = 0.1^\circ \rightarrow e_l \approx 0.35 \text{ m}$

$D = 1.0 \text{ km}: e_\alpha = 0.1^\circ \rightarrow e_l \approx 1.75 \text{ m}$

# Background



- Open-loop control

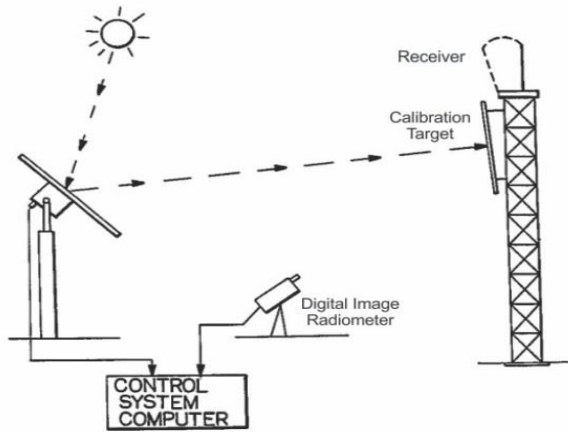


- Deterministic and non-deterministic error sources cause drift requiring calibration, which is time consuming
- No aiming feedback during operation requires drives with very tight tolerances which are costly

# Background



- Open-loop control



PS10



Gemosolar



Coalinga



Crescent D.

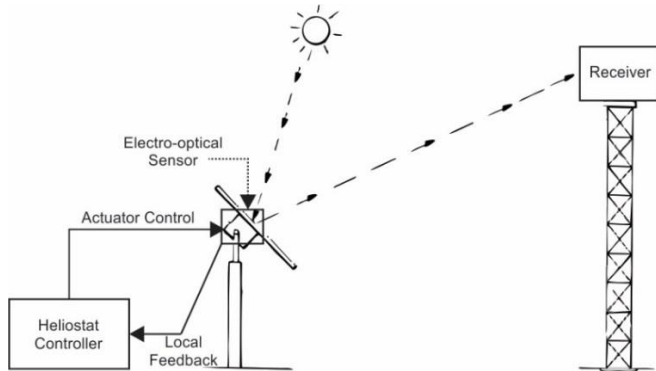


Sierra ST.

# Background



- Closed-loop (local feedback)



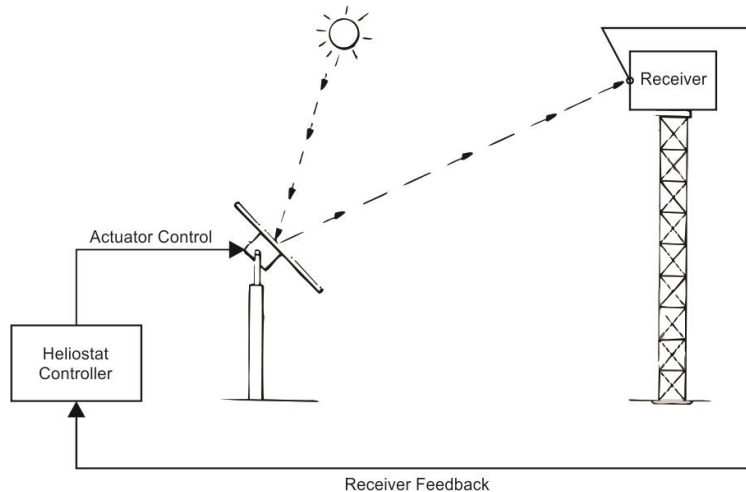
- Real-time alignment feedback negates the need for expensive drives with tight tolerances

- Mounting sensors on every heliostat can be expensive, esp. for large helio. fields

# Background



- Closed-loop (“Receiver” feedback)



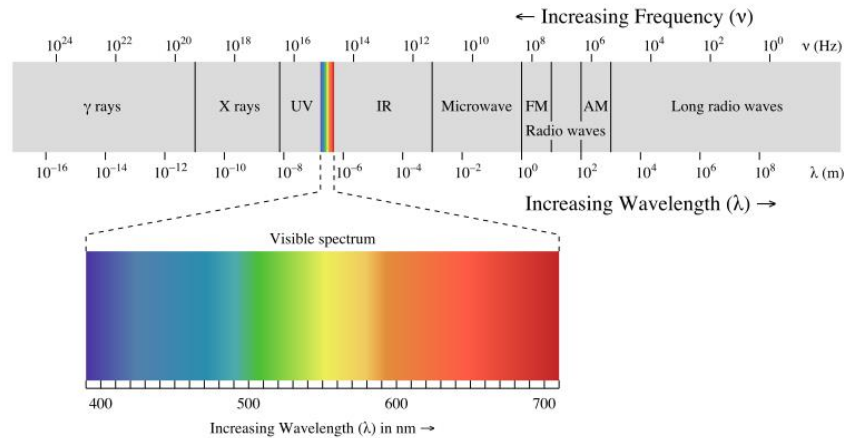
- Real-time alignment feedback negates the need for expensive drives with tight tolerances
- Does not require sensors on every heliostat
- Multiple/All heliostats can be controlled simultaneously



# Diffraction



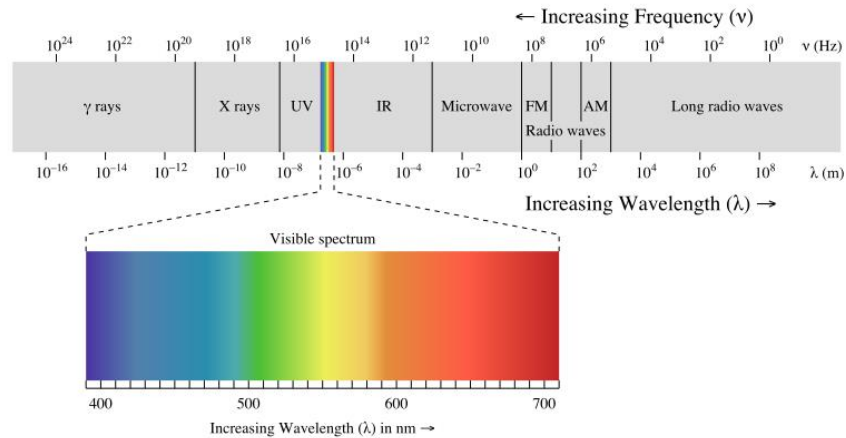
- Electromagnetic Spectrum



# Diffraction



- Electromagnetic Spectrum

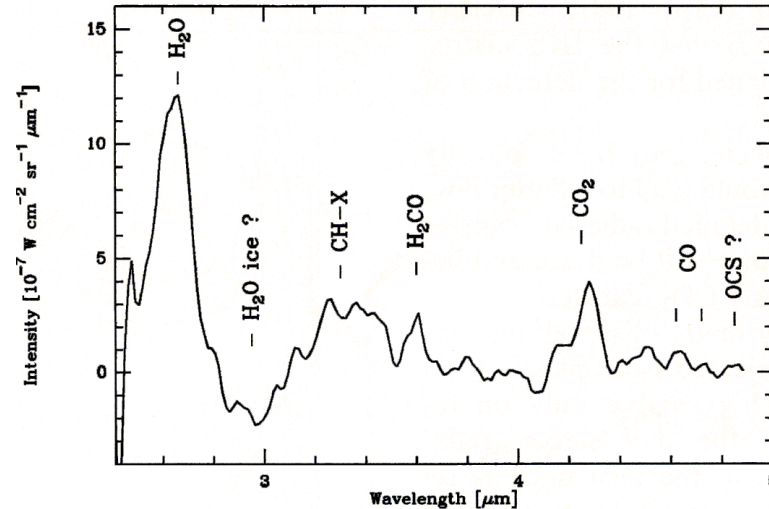
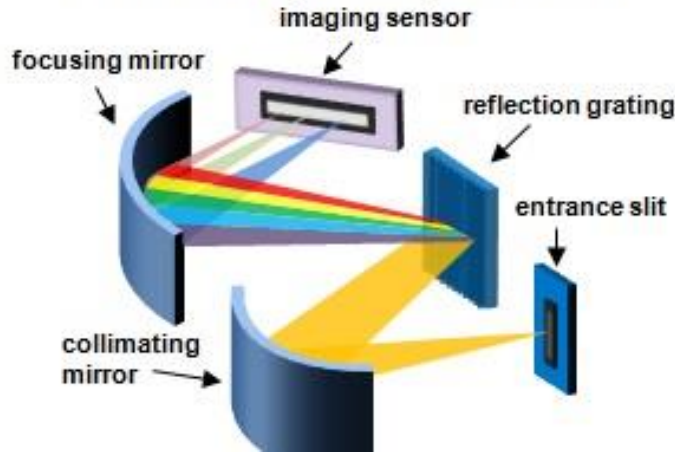


# Diffraction

- Spectroscopy



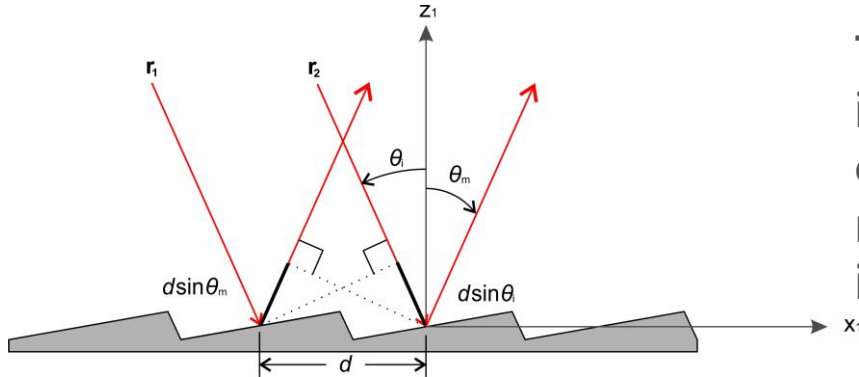
Traditional Optical Spectrometer



# Diffraction



- Diffraction gratings: Interference



The path difference between  $r_1$  and  $r_2$  is  $d \sin \theta_m + d \sin \theta_i$ . If this difference is equal to the wavelength  $\lambda$  (or a multiple,  $m\lambda$ , thereof),  $r_1$  and  $r_2$  will interfere constructively:

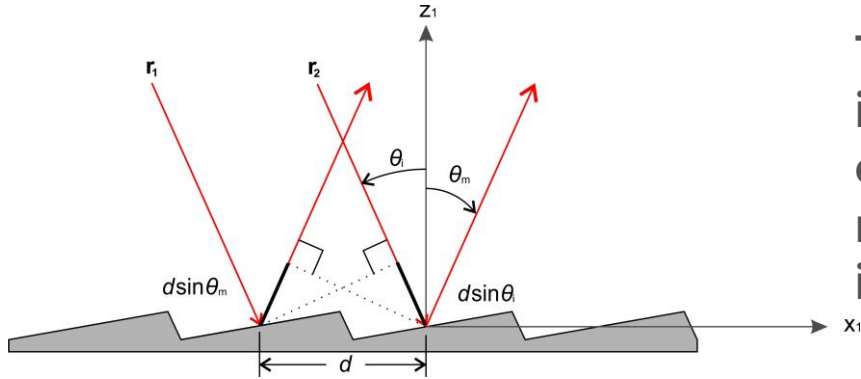
$$d \sin \theta_m + d \sin \theta_i = m\lambda \quad m = 0, \pm 1, \pm 2 \dots$$

$$\theta_m(\lambda) = \sin^{-1} \left( \frac{m\lambda}{d} - \sin \theta_i \right)$$

# Diffraction



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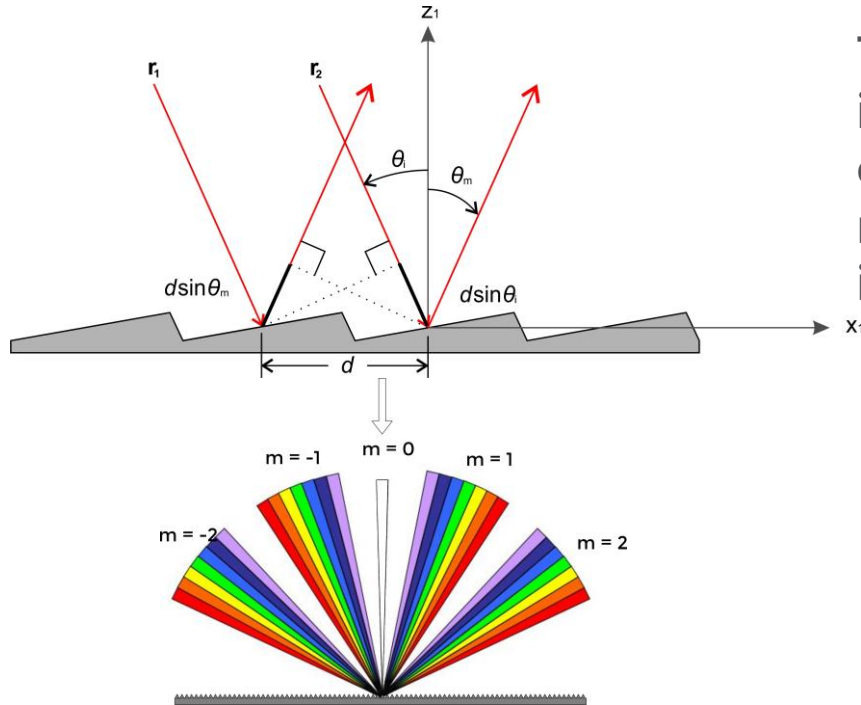
$$\theta_m(\lambda) = \sin^{-1} \left( \frac{m\lambda}{d} - \sin \theta_i \right)$$

	m=0	m=1	m=2
$\theta_m(473 \text{ nm})$	$0^\circ$	$13.7^\circ$	$28.2^\circ$

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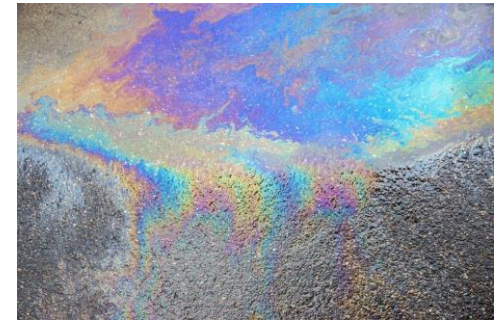
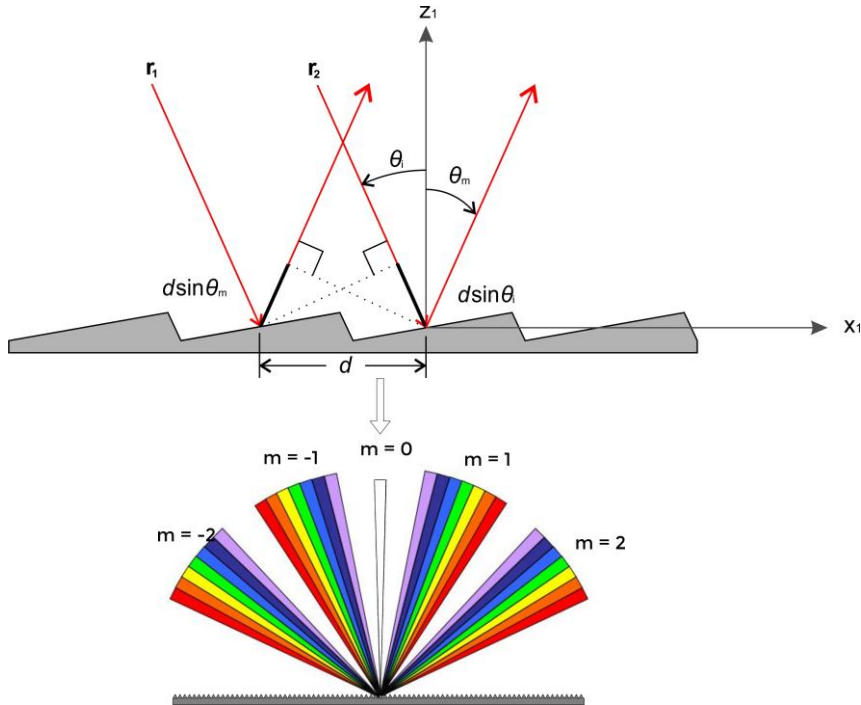
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# Diffraction



- Diffraction gratings: Interference

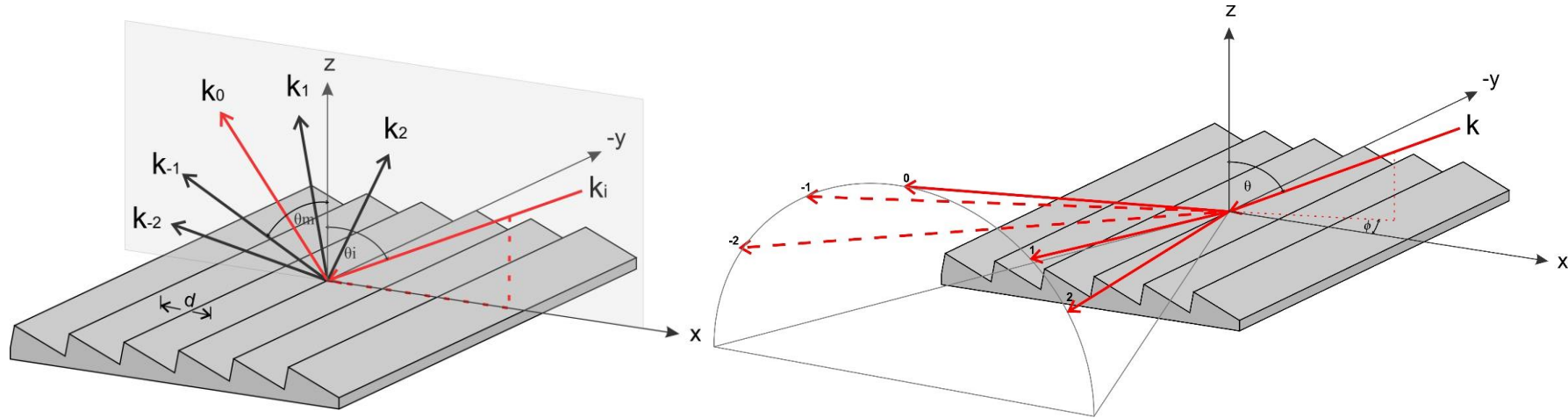


	$m=0$	$m=1$	$m=2$
$\theta_m(473 \text{ nm})$	$0^\circ$	$13.7^\circ$	$28.2^\circ$

# Diffraction



- 1-D (Linear) diffraction grating



$$\sin \theta_m = \sin \theta_i + m \frac{\lambda}{d}$$

$$\cos \phi_i (\sin \theta_m - \sin \theta_i) = \frac{m\lambda}{d}$$

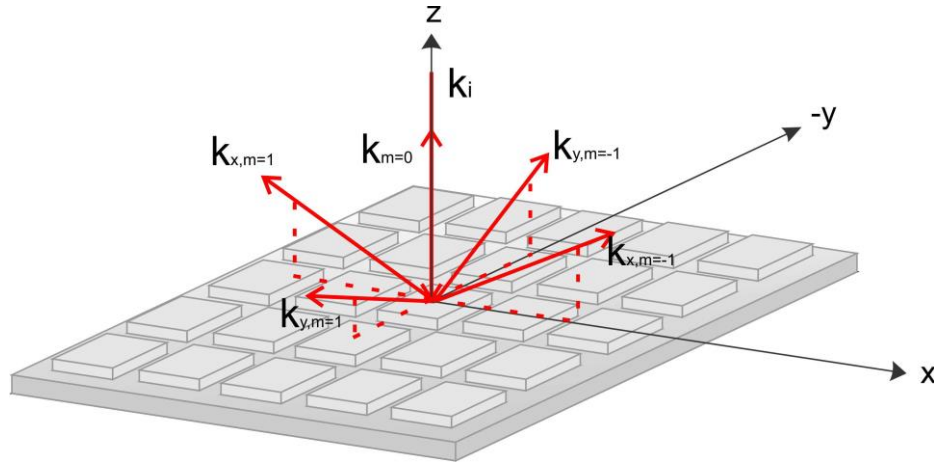
$$d(\sin \phi_m - \sin \phi_i) = 0$$



# Diffraction



- Crossed (2-D) diffraction gratings

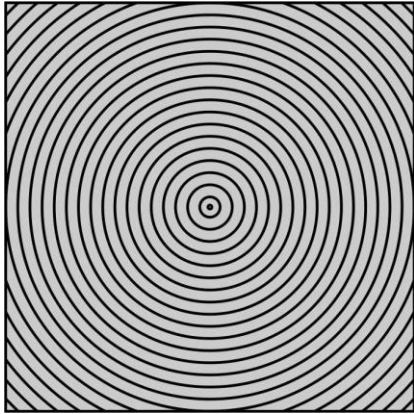


Diffraction orders will propagate in two directions, but the vector sum of the surface components of the diffraction orders in each direction represent another propagation direction.

# Diffraction



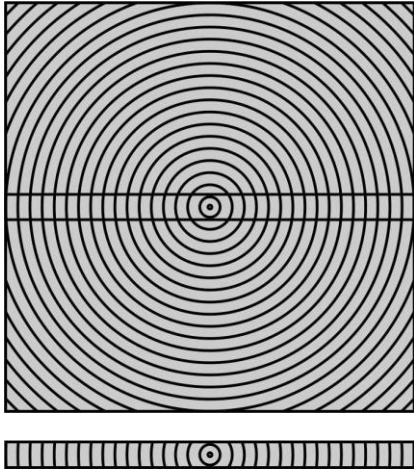
- Circular diffraction grating



# Diffraction



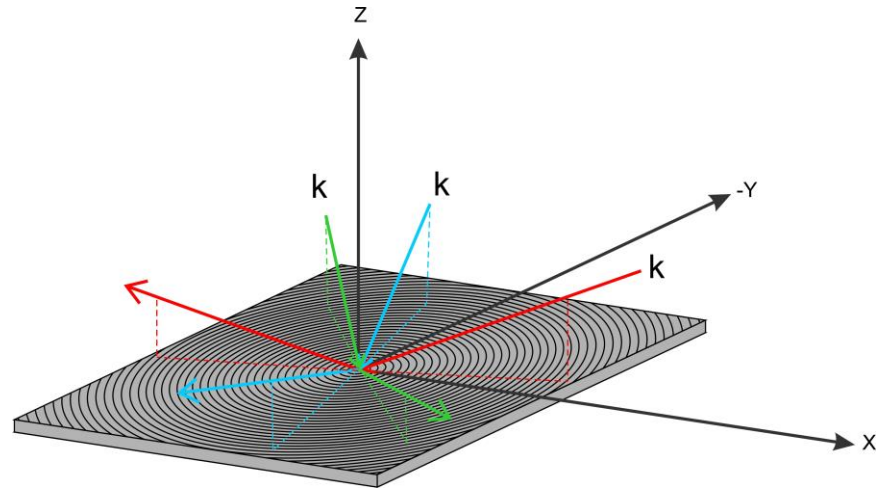
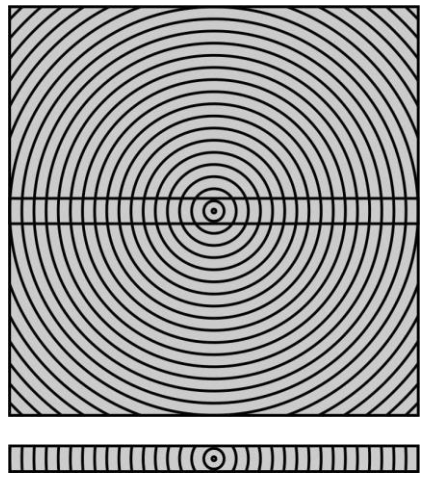
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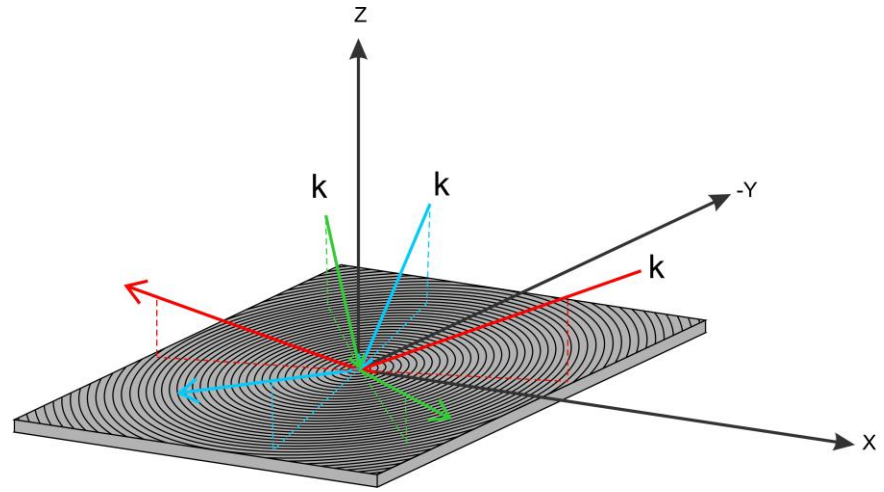
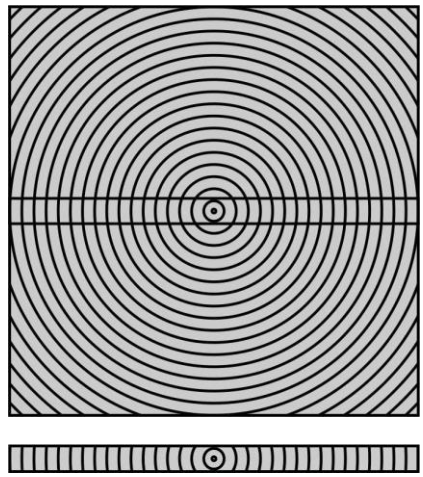
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# Diffraction



- Circular diffraction grating

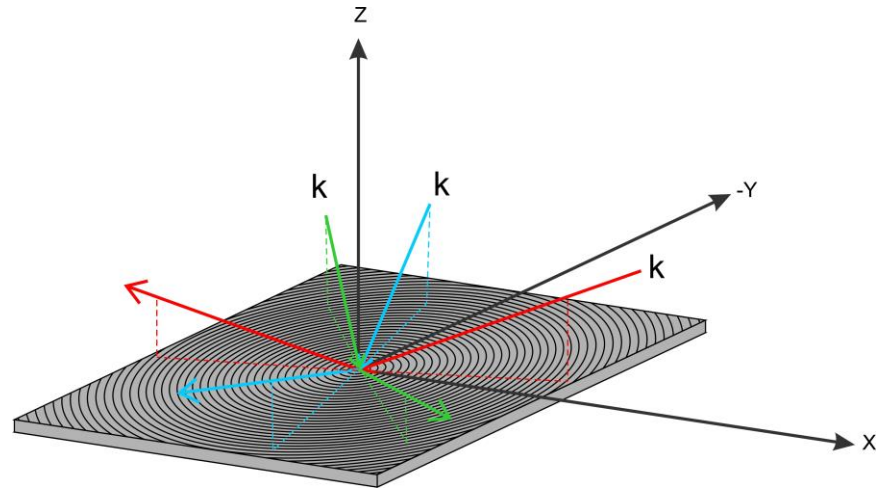
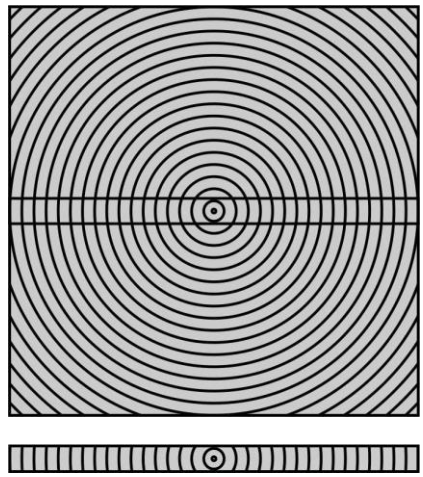


$$\sin \theta_m = \sin \theta_i + m \frac{\lambda}{d}$$

# Diffraction



- Circular diffraction grating

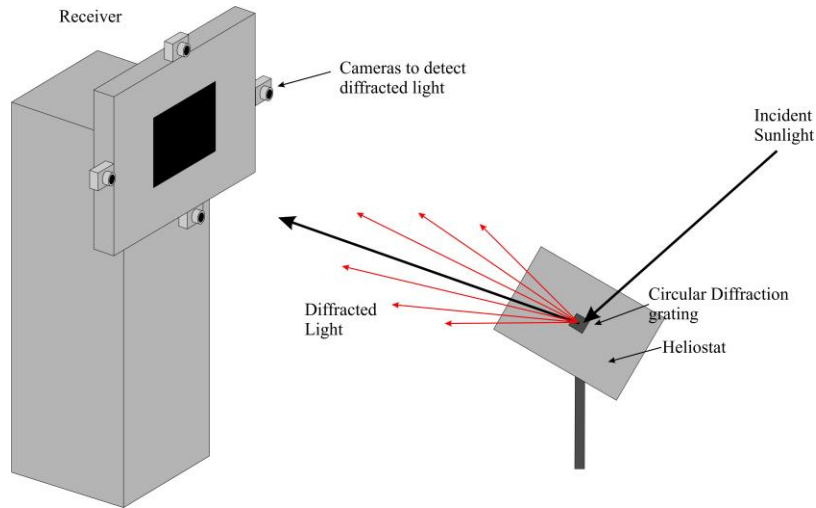


$$\sin \theta_m = \sin \theta_i + m \frac{\lambda}{d}$$

# Method



## • Overview



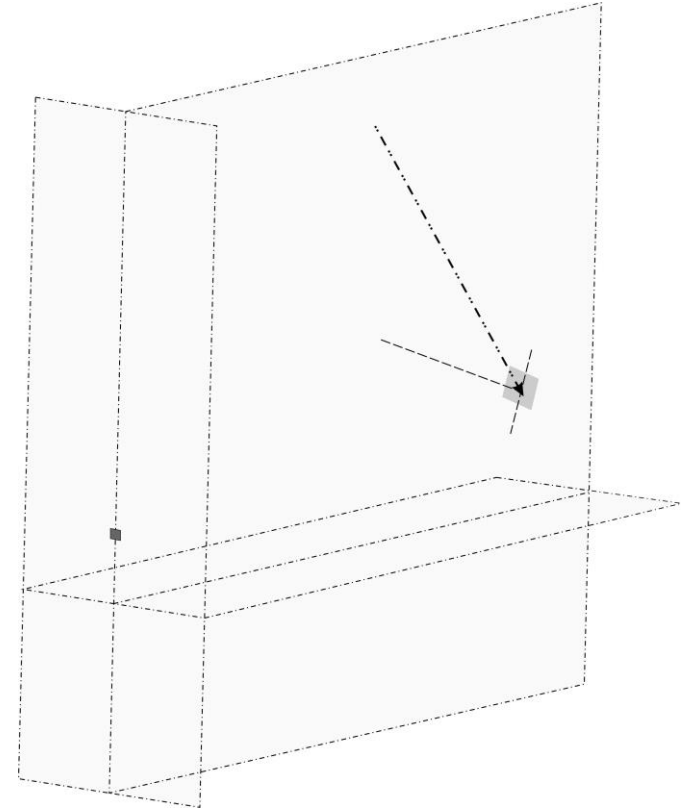
- Aim: Determine direction of the zeroth propagation order (direction of the zeroth propagation order coincides with the reflected beam).
- Camera senses the colour of diffracted light from some propagation order (1<sup>st</sup>), infers wavelength
- The light diffracted in the direction of the camera has a functional relationship with the zeroth order.

# Method



- Determining  $k_{m=0}$ :  
One camera viewpoint

- 1 Camera observes diffracted light and observes a specific colour, inferring the wavelength
- Since the circular diffraction grating diffracts light into a cone, there are an infinite directions for the zeroth order reflected beam, but is constrained to lie on a surface of a cone with vertex angle  $2\theta$  and with axis along the camera-grating vector
- Set of all possible incident vectors is the reflection (Snell's law) of the set of all possible reflection vectors and therefore also lies in a cone with angle vertex  $2\theta$ . Its axis is the reflection of the camera-grating vector.



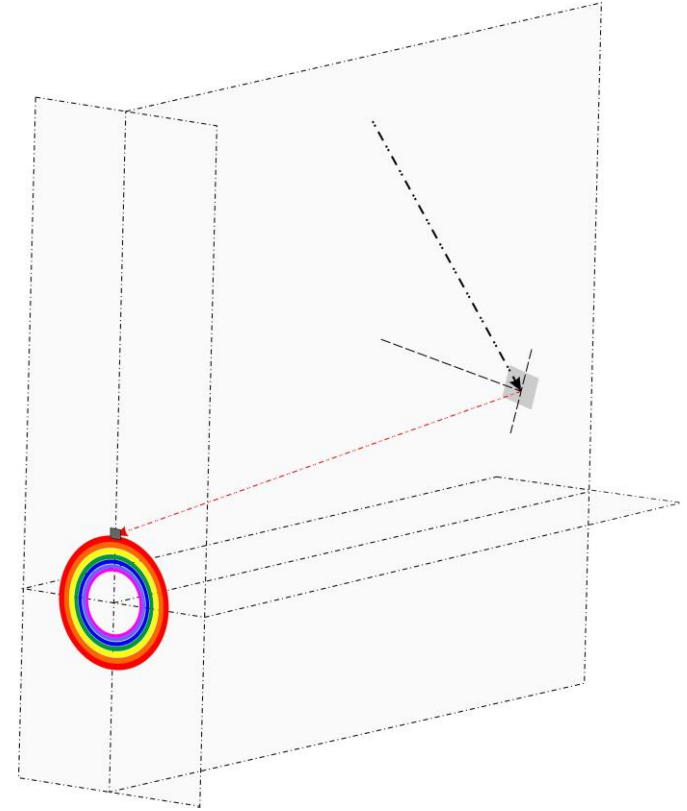


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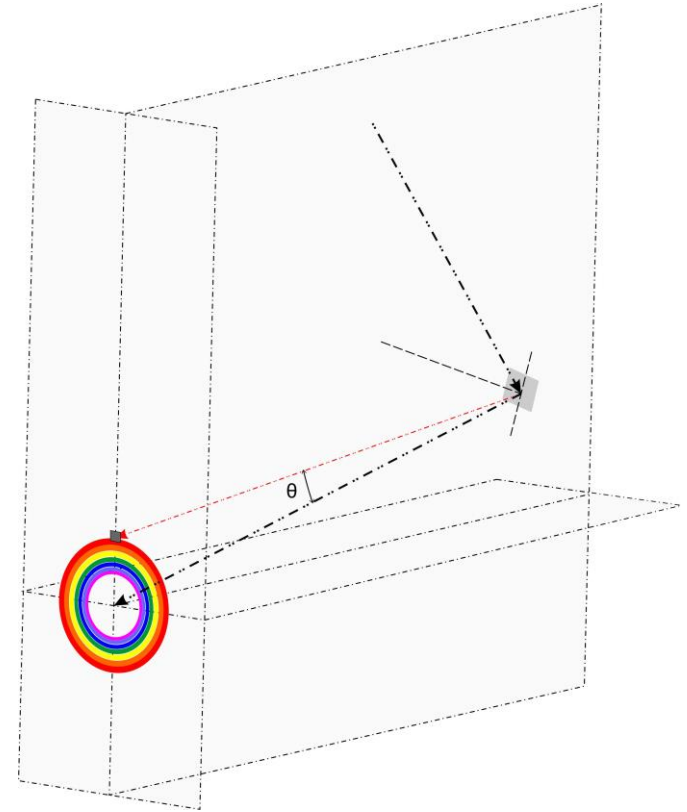


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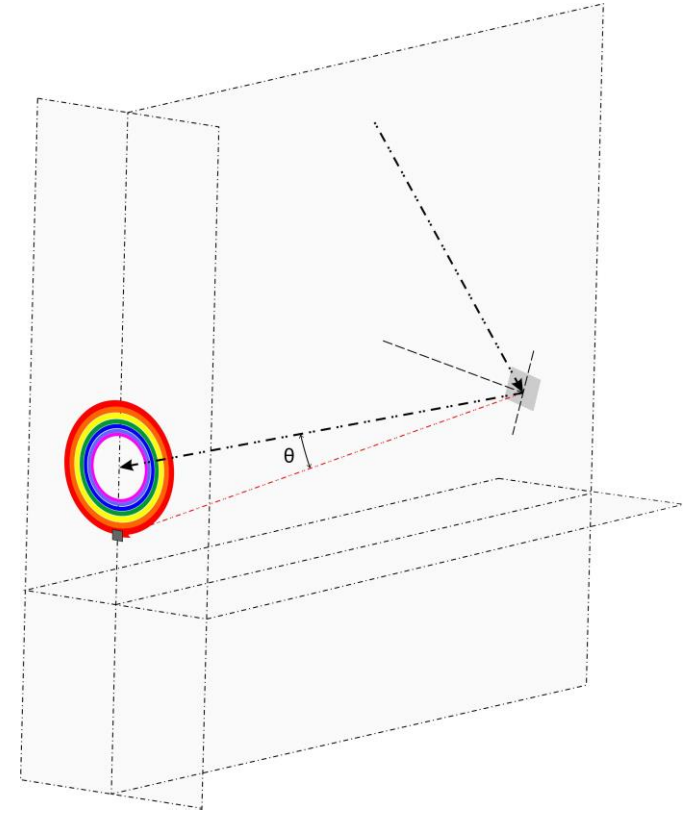


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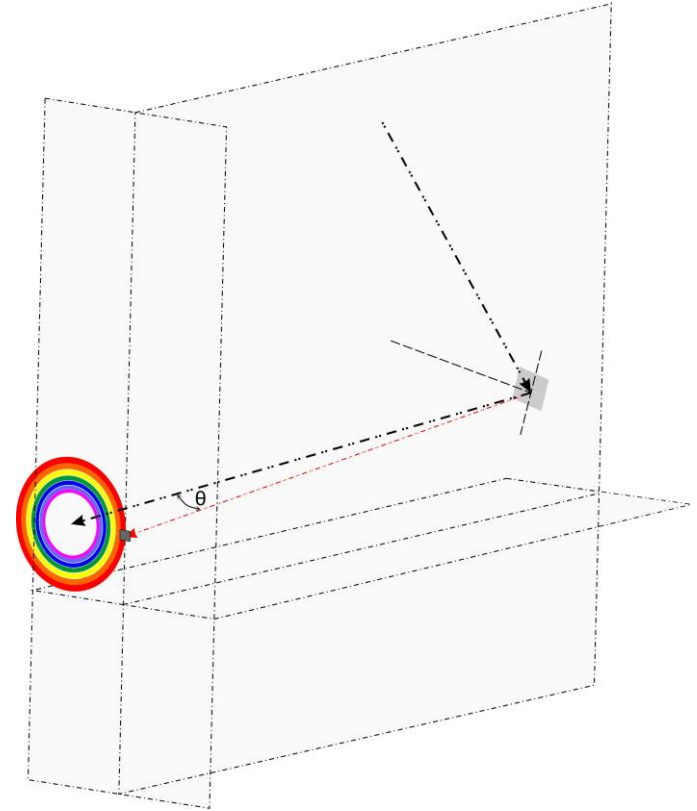


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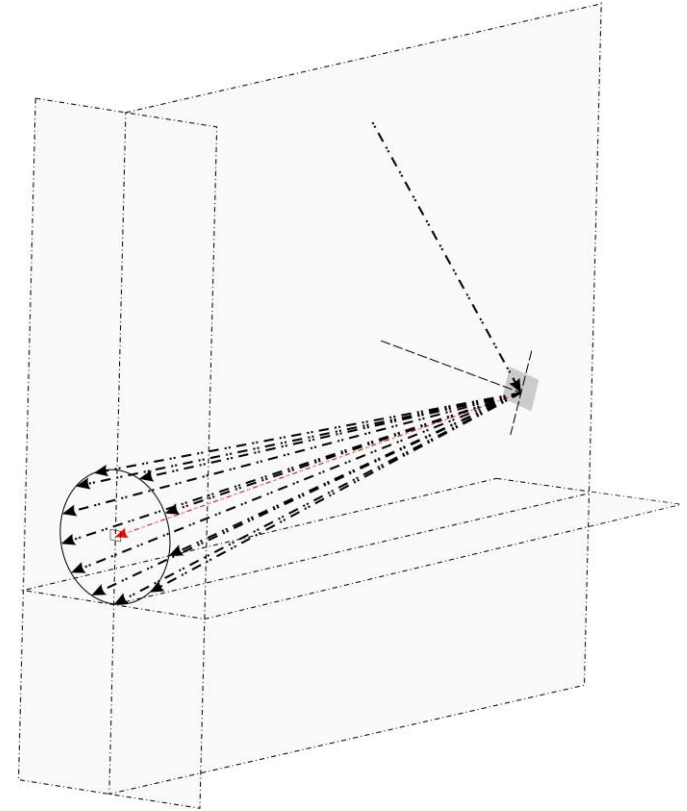


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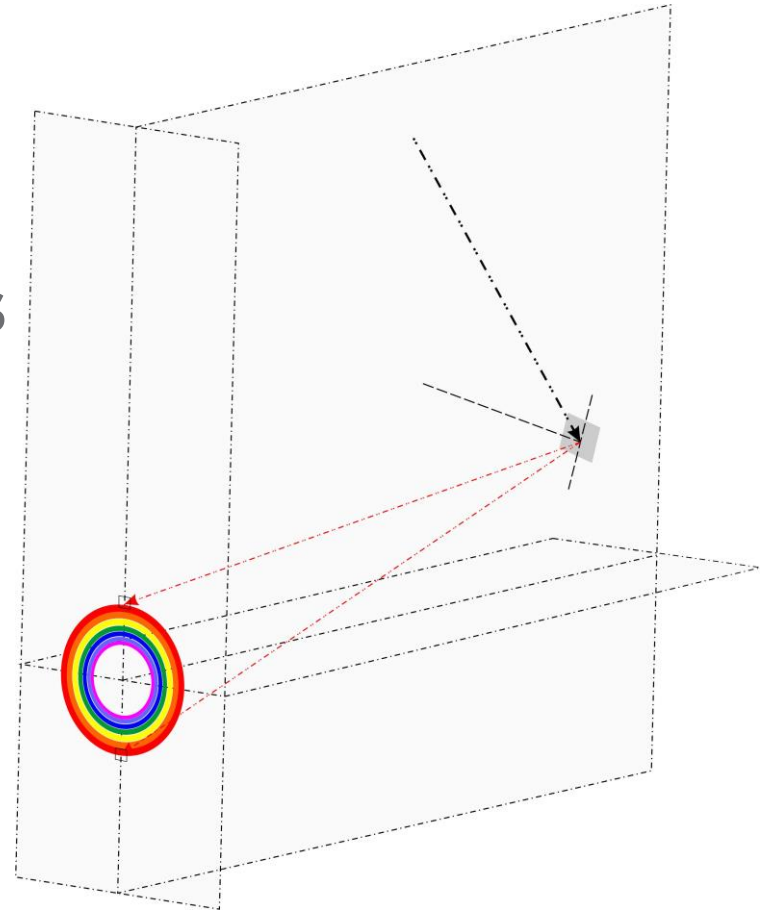


# Method

- Determining  $k_{m=0}$ :  
Two camera viewpoints

Special case: Incident light, grating normal and cameras lie in a plane.

- 2 Camera each observes diffracted light and each observes a specific colour, each inferring the wavelength.
- For each viewpoint, there are an infinite number of directions for the zeroth order reflected beam, but is constrained to lie on a surface of a cone
- The intersection of the bases of the cones is the unique solution for the direction of the zeroth order

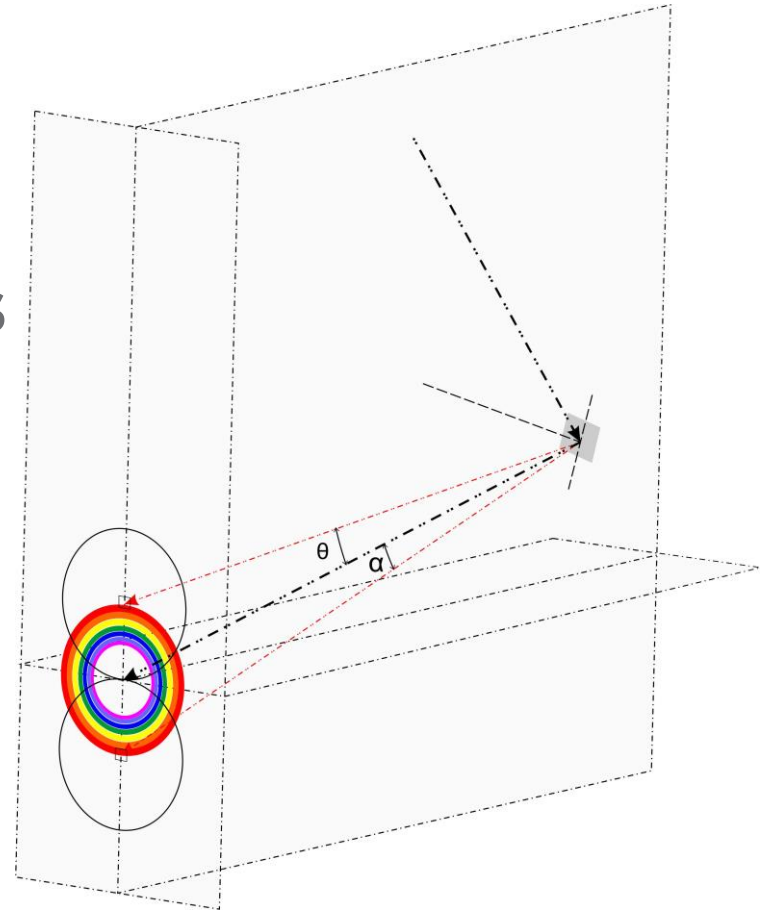


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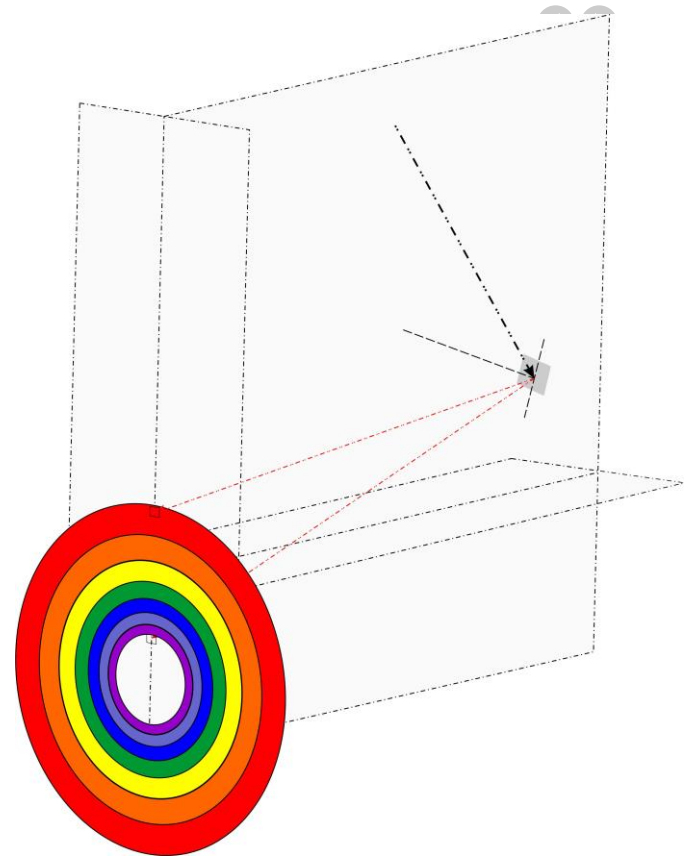


# Method

- Determining  $k_{m=0}$ :  
Two camera viewpoints

Similar special case: Incident light, grating normal and cameras lie in a plane.

- Set of possible reflection vectors for one viewpoint is encircled by the set of possible reflection vectors for the other viewpoint
- Again, the intersection of the bases of the cones is the unique solution for the direction of the zeroth order
- Can be shown that the intersection of the two circles is the unique solution for the direction of the zeroth order of the incident ray lies in the plane



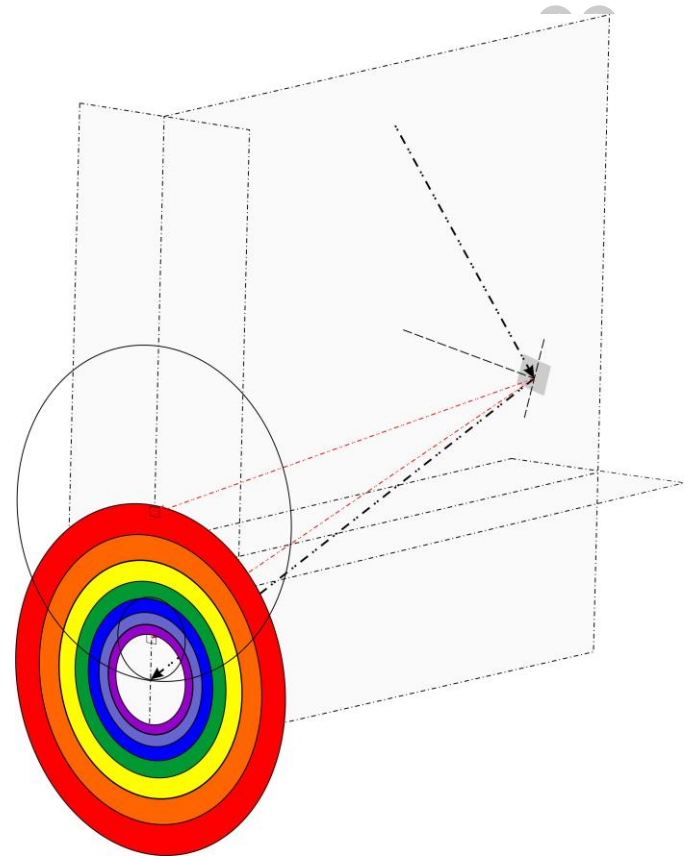


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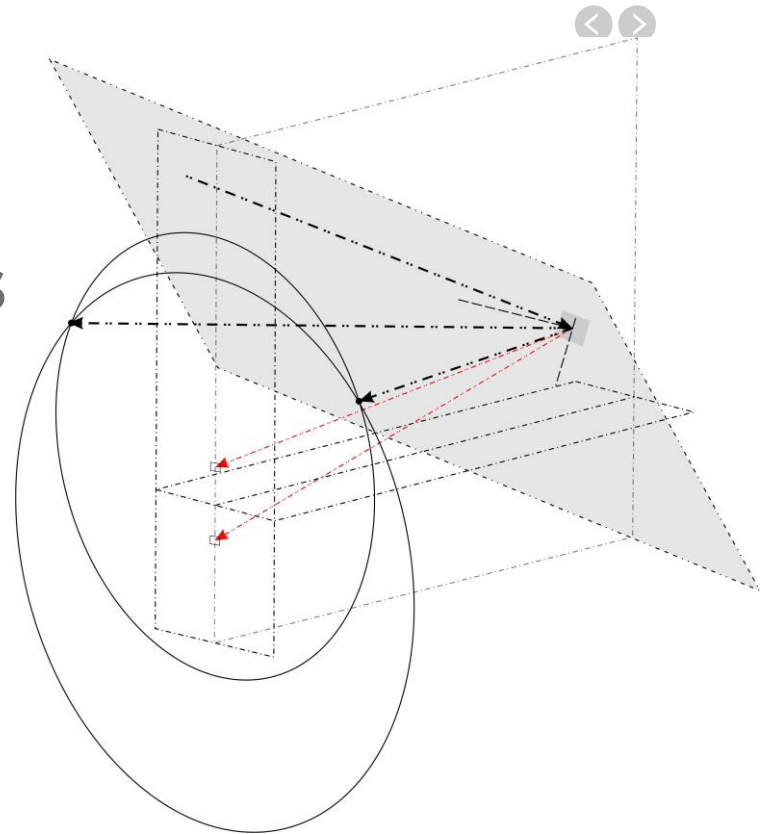


# Method

- Determining  $k_{m=0}$ :  
Two camera viewpoints

General case: Incident light lies in a an arbitrary plane

- The set of possible reflection vectors again lie along the surface of a cone for each viewpoint, but in this case there are two intersections.
- Therefore there is not a unique solution for the direction of the zeroth order vector

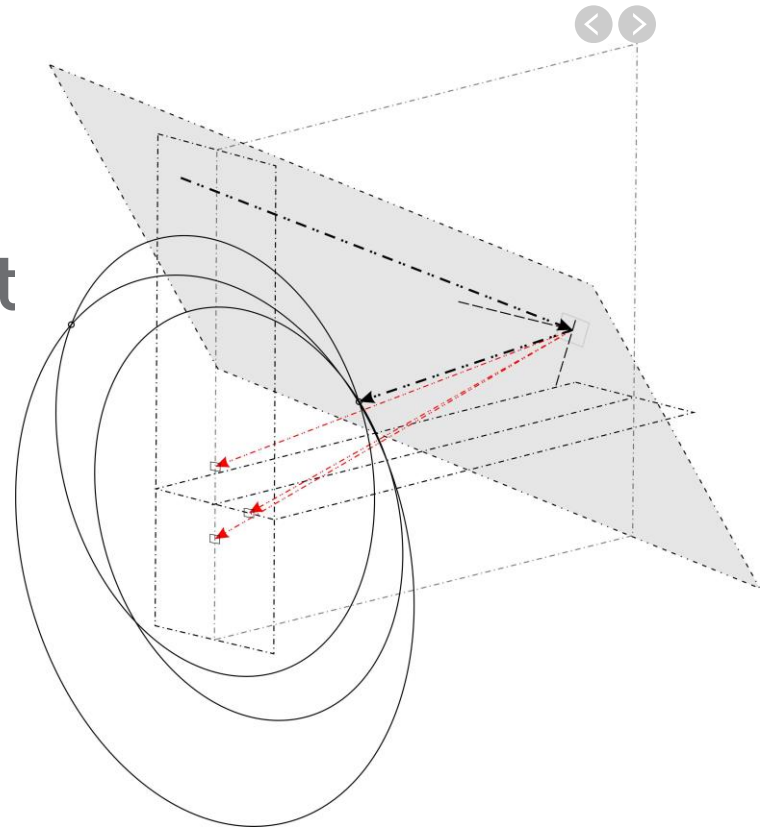


# Method

- Determining  $k_{m=0}$ :  
Three camera viewpoint

General case: Incident light lies in a an arbitrary plane

- Adding a third camera viewpoint will provide a unique solution



# Conclusion



- Design of diffraction grating
  - Propagation directions independent of grating profile
  - Profile determines the power diffracted into each order (blazing)
- Ray-trace simulation
- Experimentation

# Thank You

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Sustainable Energy Studies  
(CRSES)

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